

# Evaluating a Moist Isentropic Framework for Poleward Moisture Transport: Implications for Water Isotopes over Antarctica

Adriana Bailey<sup>1</sup>, Hansi K.A. Singh<sup>2,3</sup>, Jesse Nusbaumer<sup>4,5</sup>

<sup>1</sup>National Center for Atmospheric Research, Boulder, CO, USA

<sup>2</sup>Pacific Northwest National Laboratory, US DOE Office of Science, Richland, WA, USA

<sup>3</sup>School of Earth and Ocean Sciences, University of Victoria, Victoria, BC, Canada

<sup>4</sup>NASA Goddard Institute for Space Studies, New York, NY, USA

<sup>5</sup>Center for Climate Systems Research, Columbia University, New York, NY USA

## Key Points:

- Model experiments with water tags and isotopic tracers reveal poleward moisture transport largely follows surfaces of constant moist entropy
- Consequently, high-elevation Antarctic sites receive moisture from more equatorward sources than lower elevation sites
- The moist isentropic framework suggests shifts in moisture source regions are tightly linked to changes in temperature and rainout

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Corresponding author: Adriana Bailey, [abailley@ucar.edu](mailto:abailley@ucar.edu)

**Abstract**

The ability to identify moisture source regions and sinks, and to model the transport pathways that link them in simple yet physical ways, is critical for understanding climate today and in the past. Using water tagging and isotopic tracer experiments in the Community Earth System Model, this work shows that poleward moisture transport largely follows surfaces of constant moist entropy. The analysis not only provides insight into why distinct zonal bands supply moisture to high- and low-elevation polar sites but also explains why changes in these source regions are inherently linked to changes in temperature and rainout. Moreover, because the geometry, and specifically length, of the moist isentropic surfaces describes how much integrated rainout occurs, the analysis provides a physical framework for interpreting the isotopic composition of water in poleward-moving air, thus indicating how variations in moisture transport might influence Antarctic ice cores.

**1 Introduction**

Moisture transport by the atmospheric circulation critically regulates patterns of temperature, humidity, and precipitation. Describing this transport in simple yet physical ways can provide invaluable insight into how and why these variables change in response to climate forcing. One framework of potential appeal for evaluating outstanding questions about poleward moisture transport is a moist isentropic representation of Earth's atmospheric flow (Pauluis, Czaja, & Korty, 2008, 2010). In this framework, the atmospheric circulation is averaged on surfaces of constant moist entropy instead of a more customary vertical coordinate like pressure.

Pauluis et al. (2010) espoused this choice, arguing that a moist isentropic representation can describe the trajectories of air masses with greater fidelity if the eddies responsible for transport are largely moist adiabatic. This is approximately the case in the extratropics, where much of the poleward moisture transport is accomplished through fast-moving episodic pulses (Fajber, Kushner, & Laliberté, 2018; Laliberté & Kushner, 2014; Messori & Czaja, 2013; Newman, Kiladis, Weickmann, Ralph, & Sardeshmukh, 2012; Sinclair & Dacre, 2019). As a result, moist transport occurs on timescales faster than energy dissipation. This makes it reasonable to assume that extratropical air masses conserve energy (in the form of moist entropy) as they move poleward, even though net pole-

ward heat transport is ultimately driven by radiative imbalances between the equator and the poles. Ostensibly, one could thus use moist isentropic surfaces to define poleward moisture transport pathways and to diagnose and predict variations in moisture source regions.

Examining the accuracy of this framework is of particular interest over Antarctica, where long-standing questions about moisture source regions and sinks, and the transport pathways that link them, affect our understanding of climate today and in the past. Indeed, Lagrangian analyses of air mass trajectories (Sodemann & Stohl, 2009) and water-tagging experiments in general circulation models (GCMs; Noone & Simmonds, 2002) suggest that distinct moisture source regions supply Antarctica's low- and high-elevation sites. Consequently, there is wide geographic variation in correlations between temperature and the isotope ratios of hydrogen and oxygen in Antarctic precipitation (Goursaud, Masson-Delmotte, Favier, Orsi, & Werner, 2018; Kavanaugh & Cuffey, 2003; Masson-Delmotte et al., 2008; Sime, Wolff, Oliver, & Tindall, 2009; Yetang Wang & Jouzel, 2009)—which have traditionally informed our interpretation of past climate from ice cores. Isotopic inversion methods used to reconstruct past climate have tried to address this problem by applying a correction to the isotope-temperature relationship based on estimated conditions for the presumed evaporative source region (e.g. B. Markle, 2017; Stenni et al., 2004, 2010; Uemura et al., 2012; Vimeux, Cuffey, & Jouzel, 2002). If the average poleward moisture flow approximately conserves moist entropy, a moist isentropic framework could offer a valuable conceptual model for explaining how water isotope ratios change with simultaneous variations in moisture source region and temperature, thus bolstering our understanding of the global circulation and its ties to climate.

Here, we evaluate the utility of the moist isentropic framework for describing Antarctic moisture transport in two steps. First, we compare the source regions and transport pathways explicitly identified by water tags in GCM simulations with those indicated by moist isentropes. Second, we compare simulations of isotopic tracers in water vapor from the GCM with theoretical predictions of isotopic distillation for air mass advection along moist isentropic surfaces. Unlike water tags, simulated isotopic tracers can be compared directly with modern and historical observations.

Though ours is not the first study to relate Antarctic moisture transport and isotopic distillation to entropy, previous efforts have considered "dry" isentropic surfaces

80 alone (cf. Noone, 2008). The moist isentropic framework distinguishes itself in at least  
 81 two ways. First, it accounts for a much larger proportion of mass transport in the ex-  
 82 tratropics, since much of the moist poleward flow in dry isentropic coordinates is masked  
 83 by dry equatorward transport at low altitudes (Pauluis et al., 2008, 2010). Second, by  
 84 accounting for variations in both temperature and humidity, moist isentropes describe  
 85 the integrated rainout along moisture transport pathways more directly. Since this in-  
 86 tegrated condensation history determines the isotope ratios of water vapor and precip-  
 87 itation over Antarctica (Dansgaard, 1964), the moist isentropic framework has greater  
 88 potential to describe how variations in moisture transport influence isotopic records pre-  
 89 served in ice cores.

## 90 2 Experimental Design

91 Following previous investigations (Pauluis et al., 2008, 2010; Sherwood, Roca, Weck-  
 92 werth, & Andronova, 2010), this study uses equivalent potential temperature ( $\theta_e$ ) as a  
 93 measure of moist entropy.  $\theta_e$  is calculated using the approximation of Stull (1988):

$$\theta_e \approx \left( T + \frac{L_v}{c_{pd}} r \right) \left( \frac{p_0}{p} \right)^{R_d/c_{pd}}, \quad (1)$$

94 in which  $\theta_e$  varies principally as a function of temperature ( $T$ ), water vapor mixing ra-  
 95 tio ( $r$ ), and pressure ( $p$ ). Though the latent heat of vaporization ( $L_v$ ) and the heat ca-  
 96 pacity of dry air at constant pressure ( $c_{pd}$ ) also depend on  $T$ , because the dependence  
 97 is weak over much of the troposphere, we choose to treat these as constant and assign  
 98 them values of  $2.5 \times 10^6$  J/kg and 1006 J/kg/K, respectively.  $R_d$  is the specific gas con-  
 99 stant for dry air (287 J/kg/K), and the reference pressure ( $p_0$ ) is set to 1000 hPa. Es-  
 100 timates of  $\theta_e$  derived using the approximation suggested by Bryan (2008) were also con-  
 101 sidered, but do not alter the study's conclusions (Supporting Information). For all es-  
 102 timates of  $\theta_e$ , we use climatological values of  $T$ ,  $p$ , and  $r$ . The input variables are derived  
 103 from monthly mean output from NCAR's Community Earth System Model (CESM),  
 104 interpolated to a regular vertical pressure grid that assigns missing values, where nec-  
 105 essary, to account for surface topography.

106 To evaluate the utility of a moist isentropic framework for characterizing the source  
 107 regions that supply moisture to Antarctica and for delineating the transport pathways  
 108 by which this moisture moves poleward, two experiments are conducted. In the first ex-  
 109 periment, moisture transport pathways mapped by water tracers are compared to sur-

110 faces of constant  $\theta_e$ . Numerical water tracers are implemented in version 5 of the NCAR  
111 Community Atmosphere Model (CAM5; Neale et al., 2012) for this purpose. Atmospheric  
112 water is tagged with its region of origin (within  $10^\circ$  latitude bands over the oceans), and  
113 this tag remains through advection, phase changes, and precipitation (Singh, Bitz, Nus-  
114 baumer, & Noone, 2016). CAM5 with water tracers is run within the fully-coupled Com-  
115 munity Earth System Model (CESM1; Hurrell et al., 2013) in a 30-yr pre-industrial sim-  
116 ulation (i.e. all greenhouse gases, ozone, volcanic constituents, and solar insolation are  
117 held at pre-industrial levels), from which seasonal and annual mean climatologies are con-  
118 structed. All model components are at (nominally)  $1^\circ$  spatial resolution, and the ocean  
119 and sea ice are fully dynamic.

120 In the second experiment, we leverage the fact that, from a Lagrangian frame of  
121 reference, the isotope ratios of oxygen and hydrogen in water vapor trace the rainout of  
122 air masses, so long as air mass mixing is negligible (e.g. Noone, 2012; Worden, Noone,  
123 Bowman, the Tropospheric Emission Spectrometer science team, & data contributors,  
124 2007). (Note that air mass mixing must also be negligible for moisture transport to con-  
125 serve moist entropy). Due to their lower saturation vapor pressures, isotopically heavy  
126 water molecules (e.g.  $\text{H}_2^{18}\text{O}$ ) are preferentially removed from an air mass as condensa-  
127 tion and rainout occur. This preferential loss is well described by distillation theory (Dans-  
128 gaard, 1964). Therefore, if poleward moisture transport approximates moist isentropic  
129 advection, the isotope ratios of water vapor along the isentropes should match distilla-  
130 tion predictions.

131 To evaluate this hypothesis, we define five moist isentropic surfaces using output  
132 from CESM. The surfaces (corresponding to  $\theta_e$  values of 270, 280, 290, 300, and 310  $K$ )  
133 are derived by averaging across all meridians south of  $25^\circ$  S that share the same clima-  
134 tological  $\theta_e$  target value ( $\pm 5 K$ ) at a given pressure level. These target values were se-  
135 lected to approximate  $10^\circ$  spacing over the Southern Hemisphere extratropics; however,  
136 the results are not sensitive to the number or spacing of the moist isentropes (Support-  
137 ing Information). We then compare isotopic distillation expected for a hypothetical air  
138 mass advecting along these surfaces to the seasonally averaged oxygen isotope ratios de-  
139 rived from GCM simulations. The simulations come from an isotope-enabled version of  
140 CAM5 coupled to an isotope-enabled version of the Community Land Model (CLM4)  
141 run with prescribed sea surface temperatures, sea ice, greenhouse gases and aerosols for  
142 the years 2000-2014. Details about the model simulation and the underlying isotopic physics

143 can be found in Nusbaumer, Wong, Bardeen, and Noone (2017) and Wong, Nusbaumer,  
144 and Noone (2017).

145 Three variations of distillation are considered in order to estimate uncertainty around  
146 the isotopic predictions. For two distillation models we assume that all condensate pre-  
147 cipitates immediately, such that the heavy-to-light oxygen isotope ratio ( $R=^{18}O/^{16}O$ )  
148 decreases according to Rayleigh distillation (Dansgaard, 1964; Galewsky, Steen-Larsen,  
149 Field, Worden, & Risi, 2016):

$$R = R_0 f^{\alpha-1}, \quad (2)$$

150 where  $f$  represents the fraction of water vapor remaining (i.e.  $r/r_0$ ),  $\alpha$  is a temperature-  
151 dependent *effective* fractionation factor, and subscript 0 indicates a reference level. We  
152 assume the reference level is the pressure level immediately preceding that under con-  
153 sideration along the moist isentropic surface.  $R$  is calculated along the surface sequen-  
154 tially, using the climatological values of  $T$  and  $r$  that define the isentrope and an initial  
155 estimate from CESM of the isotope ratio at the lowest pressure level ( $R_{sfc}$ ). The first  
156 distillation model assumes that all water vapor condenses to liquid under saturated con-  
157 ditions, such that  $\alpha$  is simply the temperature-dependent *equilibrium* fractionation fac-  
158 tor ( $\alpha_{eq}$ ). In contrast, the second distillation model assumes that all water vapor deposits  
159 as ice, such that  $\alpha$  must also account for kinetic effects owing to the distinct diffusion  
160 rates of heavy and light water under supersaturated conditions ( $\alpha_{ki}$ ). We use the same  
161  $\alpha_{eq}$  formulae reported in Appendix D3 of Bolot, Legras, and Moyer (2013) for the two  
162 possible phase changes and estimate  $\alpha_{ki}$  following Nusbaumer et al. (2017). A full list  
of equations may be found in the Supporting Information.

163 The third distillation model accounts for the fact that the conversion of liquid con-  
164 densate to precipitation is not customarily 100% efficient (i.e.  $\epsilon$ =precipitation efficiency<1;  
165 see Supporting Information; Bailey, Nusbaumer, & Noone, 2015; Bailey, Toohey, & Noone,  
166 2013; Noone, 2012). The required estimates of condensate concentrations for this mod-  
167 ified distillation are derived by summing the climatological mixing ratios of liquid wa-  
168 ter and ice simulated by CESM along the moist isentropic surfaces. For  $\epsilon$ , however, we  
169 assign a fixed value of 0.5, which closely approximates the precipitation efficiency expected  
170 in atmospheric convection (cf. Lutsko & Cronin, 2018) and provides greater isotopic vari-  
171 ation from the simple Rayleigh model described above. We do not modify distillation  
172

173 for vapor conversion to ice, as low diffusion rates in ice crystals tend to inhibit isotopic  
 174 exchange with the surrounding vapor (Bolot et al., 2013; Jouzel & Merlivat, 1984).

175 As is customary, all isotope ratios are presented relative to Vienna Standard Mean  
 176 Ocean Water (VSMOW) and reported in units permil:

$$\delta = \left( \frac{R}{R_{VSMOW}} - 1 \right) \times 1000 . \quad (3)$$

177 All isotopic means are mass-weighted.

### 178 **3 Results**

#### 179 **3.1 Water Tracer Experiments**

180 We begin our evaluation of the moist isentropic framework by testing whether it  
 181 can reliably delineate the moisture source regions and transport pathways to Antarctica  
 182 identified in water tracer experiments in CESM. Figure 1a shows the relative contribu-  
 183 tions of distinct Southern Hemisphere oceanic zonal bands to the water vapor concen-  
 184 tration at various pressure levels above Antarctica. Figures 1b-g show the normalized,  
 185 zonal-mean concentrations of atmospheric water vapor evaporated from these source re-  
 186 gions, with shading demonstrating that most of the moisture evaporated from each band  
 187 follows a distinct pathway as it moves poleward. In the extratropics, these moisture plumes  
 188 approximately align with the moist isentropic surfaces indicated by contours. As a re-  
 189 sult, zonal bands farthest from Antarctica (i.e., most equatorward) tend to contribute  
 190 substantially to the upper tropospheric moisture, while higher latitudes contribute mois-  
 191 ture to the lower troposphere only (Fig. 1a). This implies that moisture evaporated from  
 192 the polar ocean (i.e. south of 60° S) is not the same water that reaches Antarctica’s high-  
 193 elevation interior (cf. Noone & Simmonds, 2002; Sodemann & Stohl, 2009). This sup-  
 194 position is confirmed by mapping both the mass-weighted mean latitudes that contribute  
 195 precipitation to Antarctica (Fig. 2a) and the mean surface moist entropy (Fig. 2b) against  
 196 the continent’s elevation contours.

197 There are, nevertheless, discrepancies between the extratropical moisture transport  
 198 pathways identified in the water-tagging experiment and the surfaces of constant moist  
 199 entropy. In particular, moisture plumes in Figs. 1c-f show an apparent southward shift  
 200 above approximately 800 hPa, indicating some degree of cross-isentropic mixing. In ad-  
 201 dition, moisture evaporating from more poleward zonal bands appears more likely to slope

202 down and cross from higher to lower moist isentropes than moisture evaporating from  
203 the subtropics. We suspect three factors may be at work.

204 First, because moist isentropes are not zonally uniform, a perfect match with the  
205 zonal water tags is not expected. It is also possible that non-entropy-conserving processes  
206 play a role. Moisture recharge by evaporation, for example, will increase the  $\theta_e$  of air masses  
207 that are fully or partially coupled to the ocean surface (i.e. those at relatively low al-  
208 titudes). Similarly, water loss through precipitation can decrease the  $\theta_e$  of rising air. How-  
209 ever, given the relative insensitivity of  $\theta_e$  to precipitation (Pauluis et al., 2010), a more  
210 likely possibility is that radiative cooling at higher altitudes is sufficient to elicit ‘down-  
211 gradient’ tendencies in poleward-moving air (Yamada & Pauluis, 2016). Previous stud-  
212 ies have shown that atmospheric energy transport is well described by diffusion down  
213 the meridional moist static energy gradient (e.g. Flannery, 1984; Frierson, Held, & Zurita-  
214 Gotor, 2007; Hwang & Frierson, 2010; Roe, Feldl, Armour, Hwang, & Frierson, 2015; Siler,  
215 Roe, , & Armour, 2018) and that extratropical potential temperature anomalies move  
216 slightly down the moist entropy gradient in the latitude-height plane (Fajber et al., 2018).  
217 Examining to what extent net atmospheric heat transport can be deduced from discrep-  
218 ancies between the actual transport pathways and the moist isentropic predictions —  
219 particularly in different climate states—would thus be an interesting direction for future  
220 research.

### 221 3.2 Isotopic tracer experiments

222 To further evaluate the conceptual accuracy and utility of the moist isentropic frame-  
223 work, we compare June-July-August (JJA) zonal-mean isotope ratios simulated in CESM  
224 along five moist isentropic surfaces with water vapor isotope ratios predicted from Rayleigh  
225 distillation during air mass advection (Fig. 3). The GCM values fall well within the bounds  
226 of the isotopic predictions, given the range of microphysical possibilities represented by  
227 the three distillation models considered. Moreover, while there are clear differences among  
228 the distillation predictions, due to variations in effective fractionation ( $\alpha$ ) or the degree  
229 of precipitation efficiency ( $\epsilon$ ), the resultant isotopic differences at high latitudes are smaller  
230 than those produced when crossing from one moist isentropic surface to the next. In par-  
231 ticular, variations in  $\epsilon$  make little difference except in the driest parts of the atmosphere  
232 (Fig. 3c), such as one might find over the highest elevations of the Antarctic continent.  
233 However, because low mixing ratios (which make up the isotope ratio denominator) tend



234 to accentuate small isotopic inaccuracies, it is difficult to gauge whether these results con-  
235 firm the importance of microphysical factors in regulating water isotope ratios in extremely  
236 cold and dry climates, as others have argued (Schoenemann, Steig, Ding, Markle, & Schauer,  
237 2018). Regardless, for the extratropics as a whole, Fig. 3 shows that the dynamics that  
238 set the geometry of the moist isentropic surfaces are the more important constraint on  
239 the atmosphere's zonal-mean isotopic composition.

240 Figure 4 emphasizes the importance of the moist isentrope geometry by showing  
241 the seasonal shift in water vapor isotope ratios along the  $\theta_e$  surfaces. As austral winter  
242 (JJA) gives way to summer (December-January-February, DJF), the surfaces are dis-  
243 placed nearly  $10^\circ$  poleward, contracting and shortening as a result. It is this change in  
244 surface shape—and specifically length—that matters most for the shift in isotopic com-  
245 position (tens of permil over Antarctica). Figure 4b illustrates this point by consider-  
246 ing the effects of seasonal variations in the individual factors that control distillation along  
247 the moist isentropes: namely, the isotopic composition of the moisture source, the effec-  
248 tive rainout along the moisture trajectory, and the temperature at which condensation  
249 occurs. These factors are represented by  $R_{sfc}$ ,  $f$ , and  $\alpha_{eq}$ —the full set of inputs required  
250 for Equation 2 under the assumptions of Rayleigh distillation. The broken lines in Fig.  
251 4b indicate the seasonal shift in isotopic composition that occurs when DJF values are  
252 substituted for JJA values for any single factor: it is hardly detectable at most locations.  
253 What this implies is that it is primarily the length of the surface—controlling how much  
254 total rainout and distillation occurs—that influences the seasonal isotopic shift that the  
255 GCM produces. This result provides evidence that seasonal isotopic variations are tightly  
256 tied to variations in mean moisture length scale and corroborates the work of Feng, Faiia,  
257 and Posmentier (2009), who argued that precipitation  $\delta^{18}O$  seasonality depends on the  
258 zonal position of the subtropical highs and coincident global moisture source regions.

#### 259 4 Implications

260 Though mean poleward moisture transport may not be strictly moist isentropic,  
261 the results of this study provide evidence that a moist isentropic representation of the  
262 meridional flow offers a useful lens for describing moisture transport and for linking changes  
263 in transport to changes in climate. First, moist entropy provides a concise argument for  
264 why high- and low-elevation Antarctic sites are linked to distinct moisture source regions  
265 (Fig. 2; Noone & Simmonds, 2002; Sodemann & Stohl, 2009) and exhibit different isotope-

266 temperature scaling relationships geographically and temporally (Goursaud et al., 2018;  
267 Kavanaugh & Cuffey, 2003; Masson-Delmotte et al., 2008; Sime et al., 2009; Yetang Wang  
268 & Jouzel, 2009). Low-altitude polar air masses simply cannot gain enough potential en-  
269 ergy (through loss of latent and sensible heat) to reach the high-elevation continental in-  
270 terior while still conserving moist entropy. The moist isentropic framework thus reinforces  
271 the findings of earlier studies by Noone and Simmonds (2002) and Noone (2008), which  
272 argued that low buoyancy and potential temperature limit the influence of evaporation  
273 from Antarctica’s coastal waters on the moisture budget—and hence isotopic records—  
274 of ice core drilling sites on the Antarctic plateau.

275 Observed isotope ratios of water vapor and precipitation from near the summit of  
276 Dome C (3233 m, Casado et al., 2016; Goursaud et al., 2018) further support this con-  
277 tention. As shown in Fig. 4a, the observed isotope ratios are simply too low to be con-  
278 sistent with advection of evaporate along the lowest  $\theta_e$  surfaces. Indeed, the water va-  
279 por measurements (collected between December 2014 and January 2015) are most con-  
280 sistent with the 300 K surface, whose affiliated source region migrates between 40° and  
281 45° S annually. The center of this zonal band aligns almost exactly with the mean an-  
282 nual moisture source latitude identified by water tags in CESM (Fig. 2a). Previous stud-  
283 ies using other tracer methods have demonstrated similar links between the mid-latitude  
284 surface and higher altitudes in the Arctic, indicating that isentropic transport can ef-  
285 fectively deliver mid-latitude pollution and warming signals to polar regions (Orbe, Holzer,  
286 Polvani, & Waugh, 2013; Orbe et al., 2015).

287 Second, our results suggest that it is not so much the differences in moisture source  
288 per se that cause Antarctica’s isotope-temperature relationships to vary with elevation,  
289 but rather the differences in total rainout dictated by the distinct  $\theta_e$  surfaces that link  
290 the source regions to these sites (Fig. 4). As clear from Equation 1, both temperature  
291 and moisture define the geometry of the atmosphere’s moist isentropic surfaces, and these  
292 variables themselves are strongly linked to one another through the Clausius-Clayperon  
293 relationship, assuming variations in relative humidity are negligible. Consequently, shifts  
294 in temperature imply a change in the latitude and pressure coordinates of the moist isen-  
295 tropes. The resultant modification to surface geometry not only affects hydrological link-  
296 ages between Antarctica and lower-latitude regions, but also influences the mean distance  
297 over which moisture is transported. Our study suggests it is this change in mean mois-

298 ture length scale that alters the total rainout experienced by poleward moving air and,  
299 ultimately, its isotopic composition.

300 Finally, our analysis helps demonstrate the utility of idealized distillation models  
301 by elucidating why these models work despite their simplicity. Because mixing is a cross-  
302 isentropic process, distillation can provide fairly accurate predictions of isotopic changes  
303 if the moisture transport pathways considered mostly conserve moist entropy, as we have  
304 shown is the case in the extratropics. Conversely, because moist (as compared to dry)  
305 isentropes account for variations in both temperature and precipitable water with alti-  
306 tude, they offer a useful conceptual framework for predicting and interpreting isotopic  
307 distillation with poleward transport for a given climate state.

## 308 5 Conclusion

309 Using a single state-of-the-art GCM, this study shows that poleward moisture trans-  
310 port is largely consistent with a moist isentropic view of the mean atmospheric flow. Both  
311 numerical water tracer and isotopic tracer experiments in the Community Earth Sys-  
312 tem Model (CESM) demonstrate that moist entropy is a useful framework for identify-  
313 ing the moisture source regions that supply moisture to Antarctica and for delineating  
314 the hydrological pathways by which moisture sources and sinks are linked. The fact that  
315 our results are self-consistent between the distinct tracer experiments adds a degree of  
316 confidence to the results, though further evaluation, using other GCMs and targeted ob-  
317 servational campaigns, would be desirable. The isotopic results are particularly valuable  
318 in that they can be compared directly to observations, whether remote or in situ (e.g.  
by aircraft).

320 The moist isentropic framework provides a simple yet physical explanation for a  
321 number of key relationships. It shows, for instance, that high- and low-elevation sites at  
322 high-latitudes are connected to distinct moisture source regions, with higher-elevation  
323 sites receiving moisture from more equatorward sources, due to the shape of the moist  
324 isentropic surfaces. The surface geometry also controls the mean distance moisture trav-  
325 els by altering the integrated rainout experienced by poleward moving air. Since this to-  
326 tal rainout regulates isotopic distillation to first order, conservation of moist entropy pro-  
327 vides a conceptual basis for understanding how changes in meridional transport influ-  
328 ence the isotope ratios of water vapor over Antarctica, as others have intimated (B. R. Markle

et al., 2017; Noone, 2008; Stenni et al., 2004, 2010; Vimeux et al., 2002). Moreover, because the isentropic surface geometry is largely defined by atmospheric temperature, moist entropy offers a possible framework for predicting variations in moisture source region and moisture length scale with changes in climate.

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513 **Figure 1.** Zonal-mean moisture source regions and pathways for Southern Hemisphere atmo-  
514 spheric water vapor: **(a)** contribution of distinct oceanic zonal bands to the annual mean water  
515 vapor over Antarctica, normalized by the water vapor concentration at each pressure level; and  
516 **(b-g)** (shading) normalized, annual and zonal mean distributions of water vapor in the Southern  
517 Hemisphere sourced from (b) 60° S to the pole, (c) 50° S to 60° S, (d) 40° S to 50° S, (e) 30° S  
518 to 40° S, (f) 20° S to 30° S, and (g) 10° S to 20° S, overlaid with (contours) equivalent potential  
519 temperature (K). A representative surface pressure for Dome C, Antarctica (3233 m, discussed  
520 later in the text) is indicated by the dashed line in (a).

521 **Figure 2.** Moisture source latitudes for Antarctic precipitation and moist entropy at the  
522 surface: **(a)** annual mean latitude from which precipitation originates (degrees); and **(b)**  $\theta_e$  at  
523 the surface (K). Contours show surface elevation (m) in both panels. The black dot marks the  
524 location of Dome C observations (discussed later in the text) in panel (a).

525 **Figure 3.** Water vapor isotope ratios on moist isentropic surfaces. (a) JJA  $\delta^{18}O$  values pre-  
 526 dicted for five moist isentropic surfaces (distinguished by color and labeled in K) shown as a  
 527 function of latitude. Predictions come from (dashed line) modified distillation with a precipi-  
 528 tation efficiency ( $\epsilon$ ) of 0.5, assuming all water vapor condenses to liquid; (solid line) Rayleigh  
 529 distillation ( $\epsilon=1.0$ ), assuming all water vapor condenses to liquid; (dotted line) Rayleigh distil-  
 530 lation, assuming all water vapor deposits as ice; and (crosses) CESM. (b) Predictions from the  
 531 distillation models identified in (a) are plotted against simulated isotope ratios in water vapor  
 532 from CESM, with the 1:1 line shown in gray. (c) Differences between the various distillation  
 533 models and CESM are shown as a function of water vapor mixing ratio (g/kg), with the zero-line  
 534 shown in gray. Note the reversed y-axis in all panels.

535 **Figure 4.** Seasonal variations in water vapor isotope ratios along moist isentropic surfaces:  
 536 (a) (thin line) JJA and (thick line) DJF  $\delta^{18}O$  values predicted for five moist isentropic surfaces  
 537 (distinguished by color and labeled in K) shown as a function of latitude. Predictions come from  
 538 Rayleigh distillation assuming all water vapor condenses to liquid. Symbols show isotope ratios  
 539 from CESM and observations from Dome C, Antarctica, for comparison. The open circle with  
 541 vertical bar identifies the mean and total range of  $\delta^{18}O$  in water vapor (Dome  $C_V$ ) observed by  
 542 Casado et al. (2016) during December 2014-January 2015. The closed circle shows the annual  
 543 mean precipitation  $\delta^{18}O$  (Dome  $C_P$ ) reported by Goursaud et al. (2018). (b) Variations in the  
 544  $\delta^{18}O$  values along JJA moist isentropic surfaces produced when using DJF values for (dashed  
 545 line)  $R_{sfc}$  (the water vapor isotope ratio near the moisture source), (dotted line)  $f$  (one minus  
 546 the effective rainout along the moisture trajectory), and (dotted-dashed line)  $\alpha_{eq}$ , which is deter-  
 547 mined by atmospheric temperature. Scatterplots of DJF v. JJA values for these three factors are  
 provided in the Supporting Information.

Figure 1.

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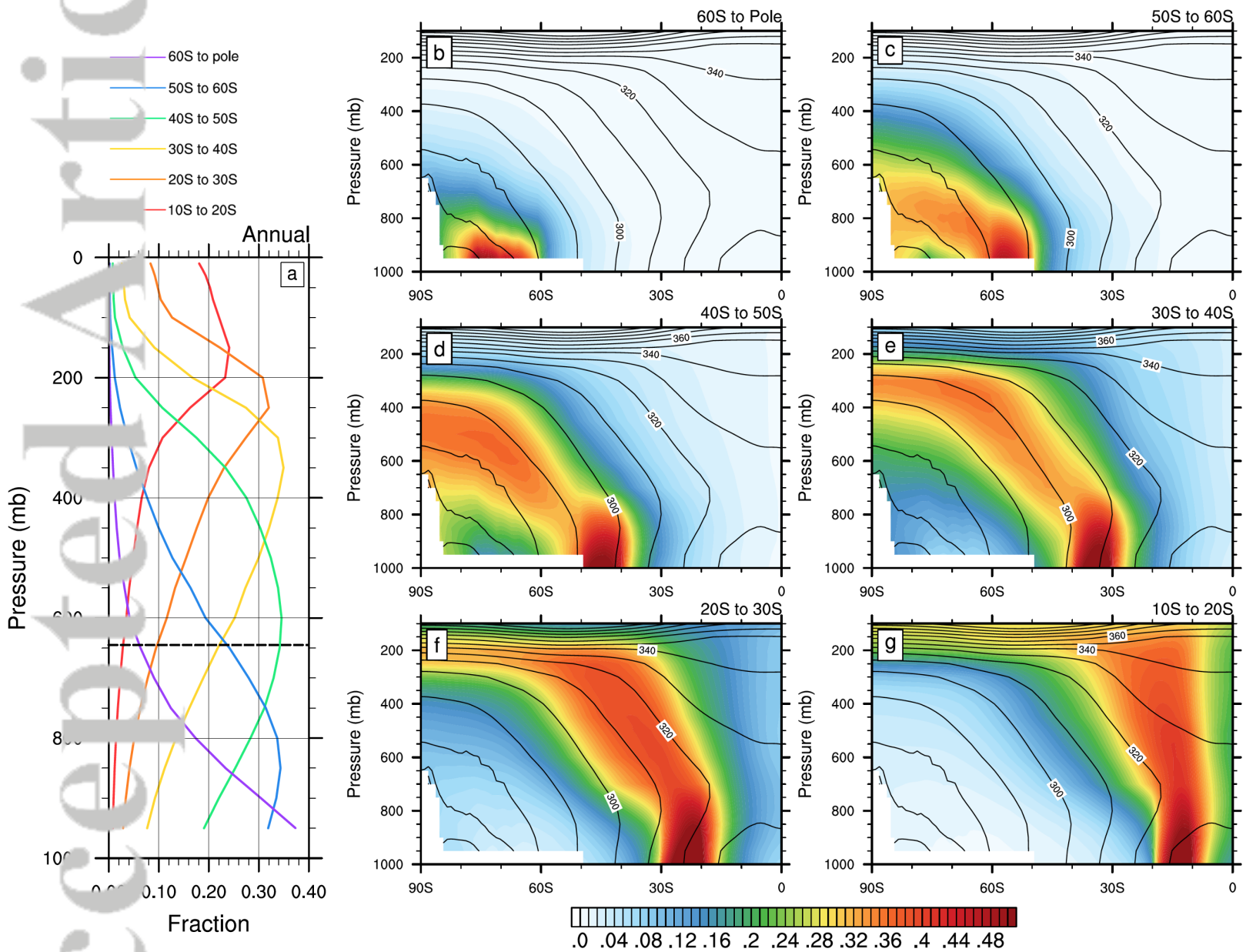


Figure 2.

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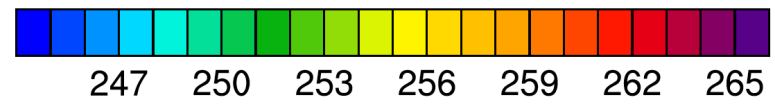
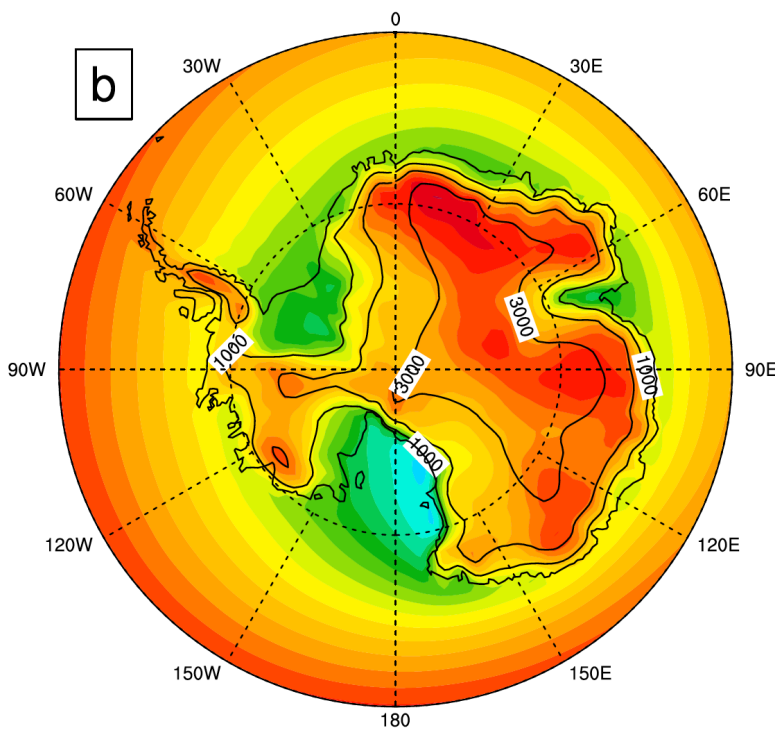
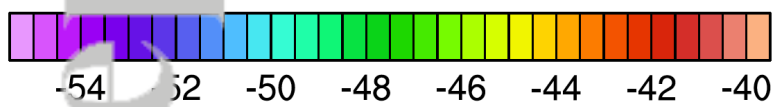
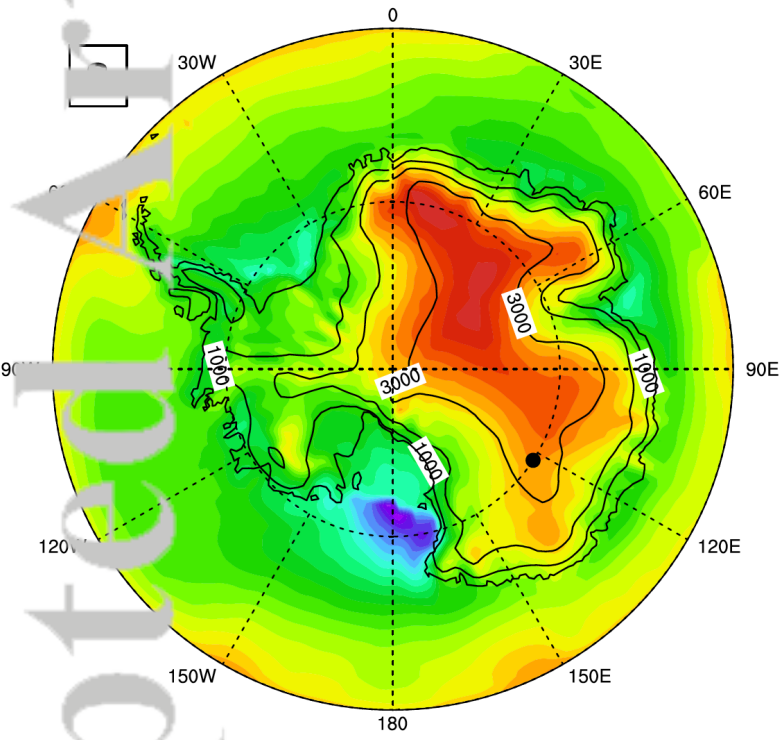


Figure 3.

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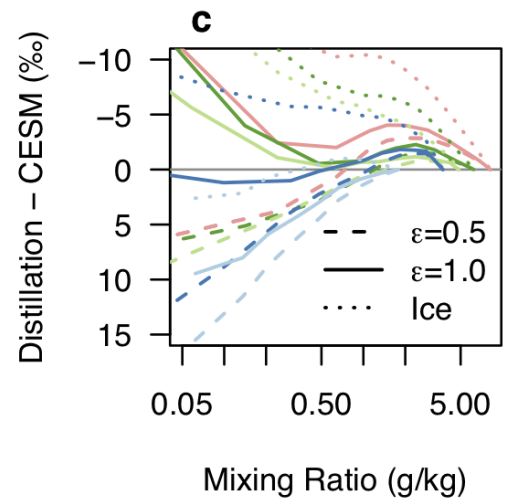
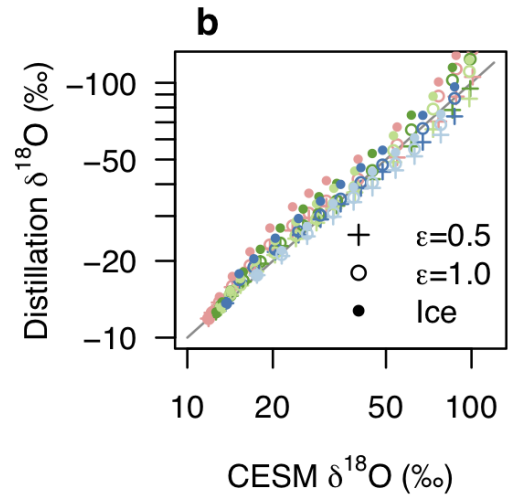
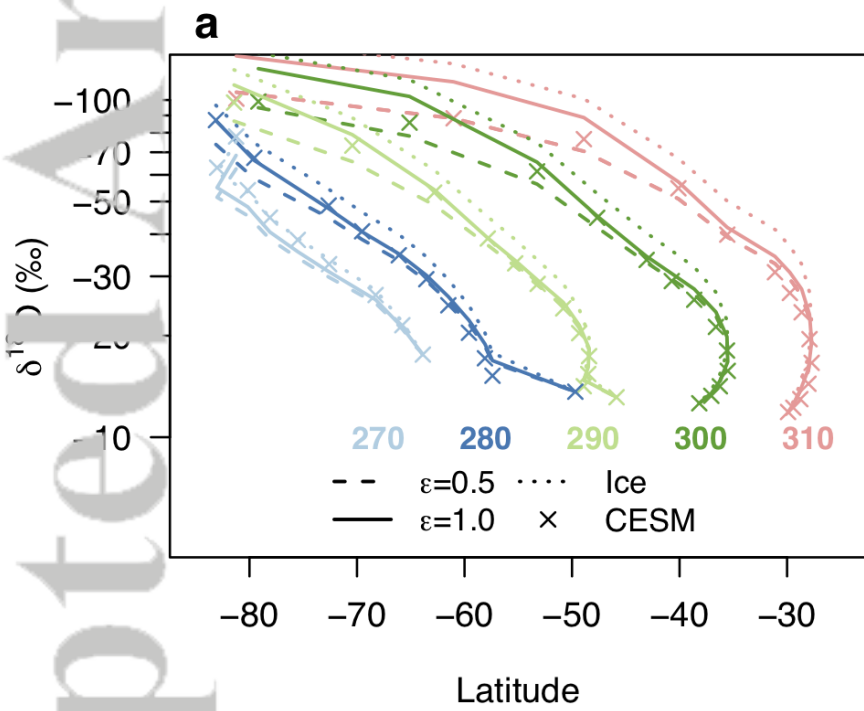
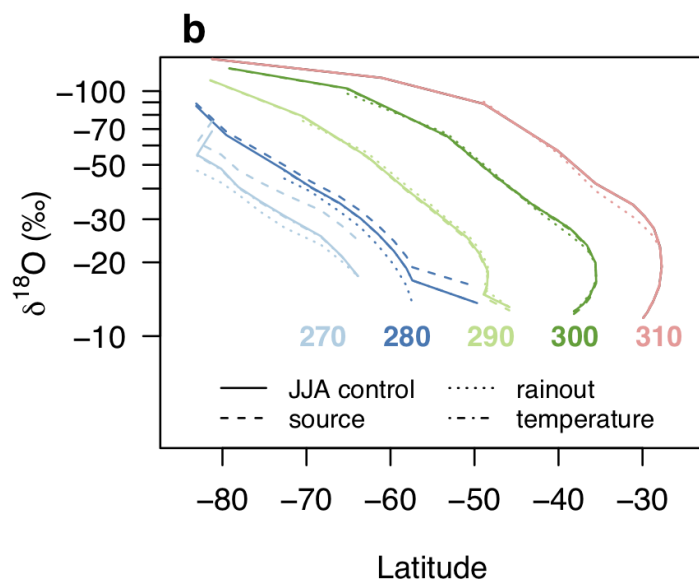
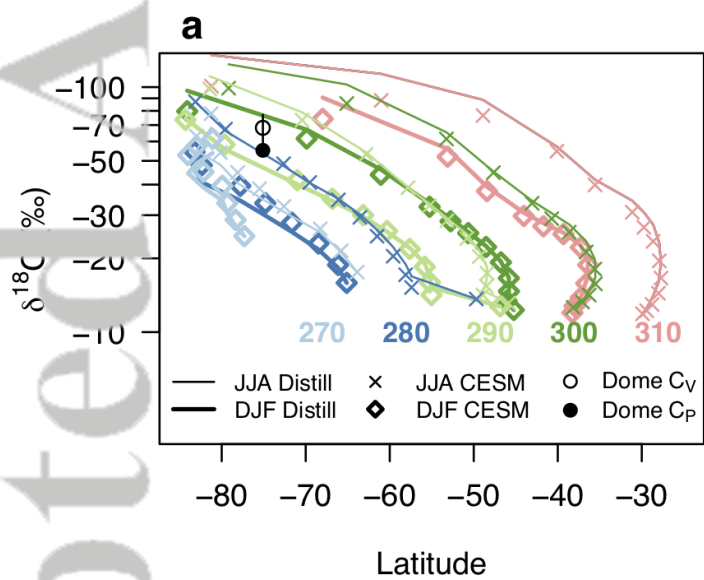
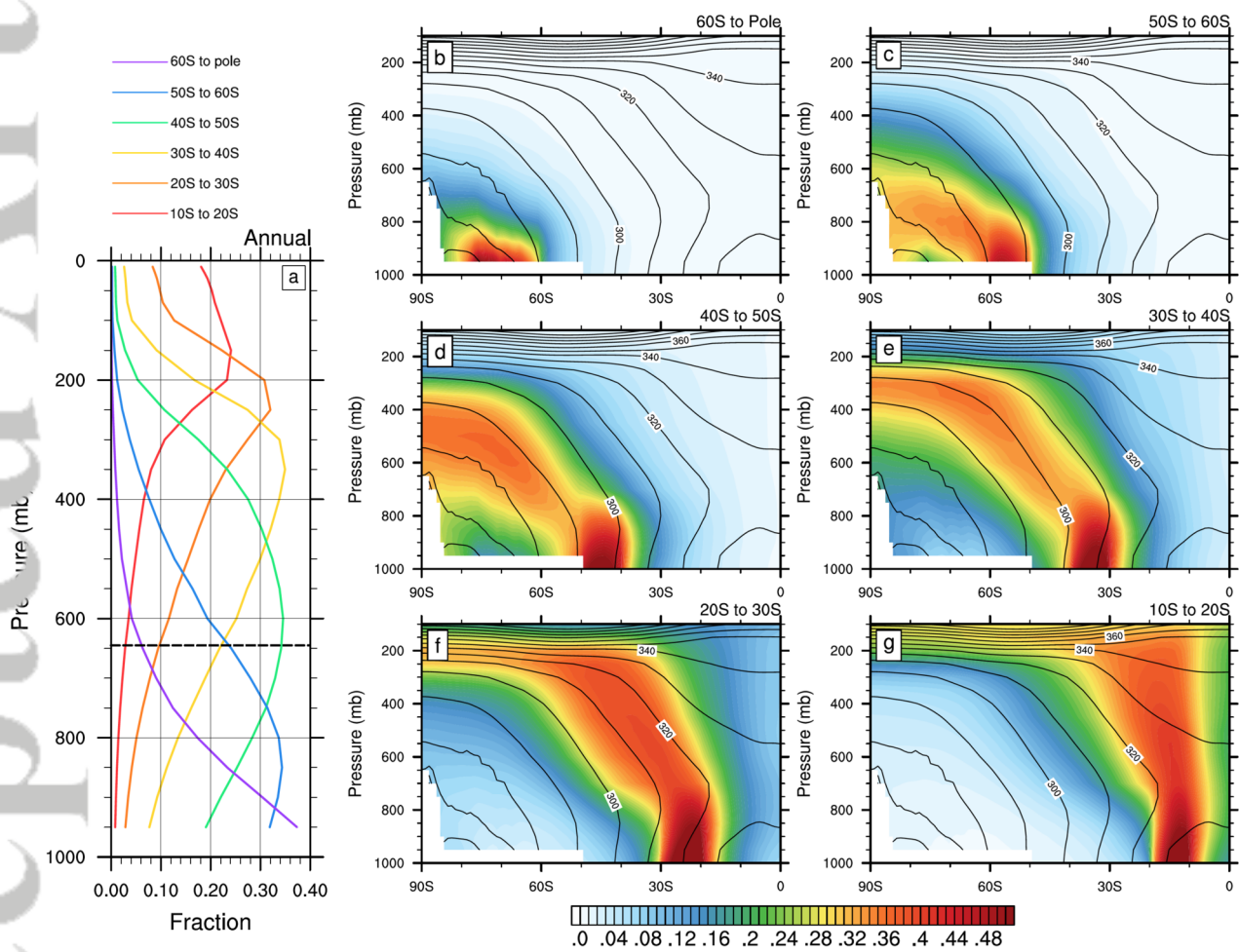


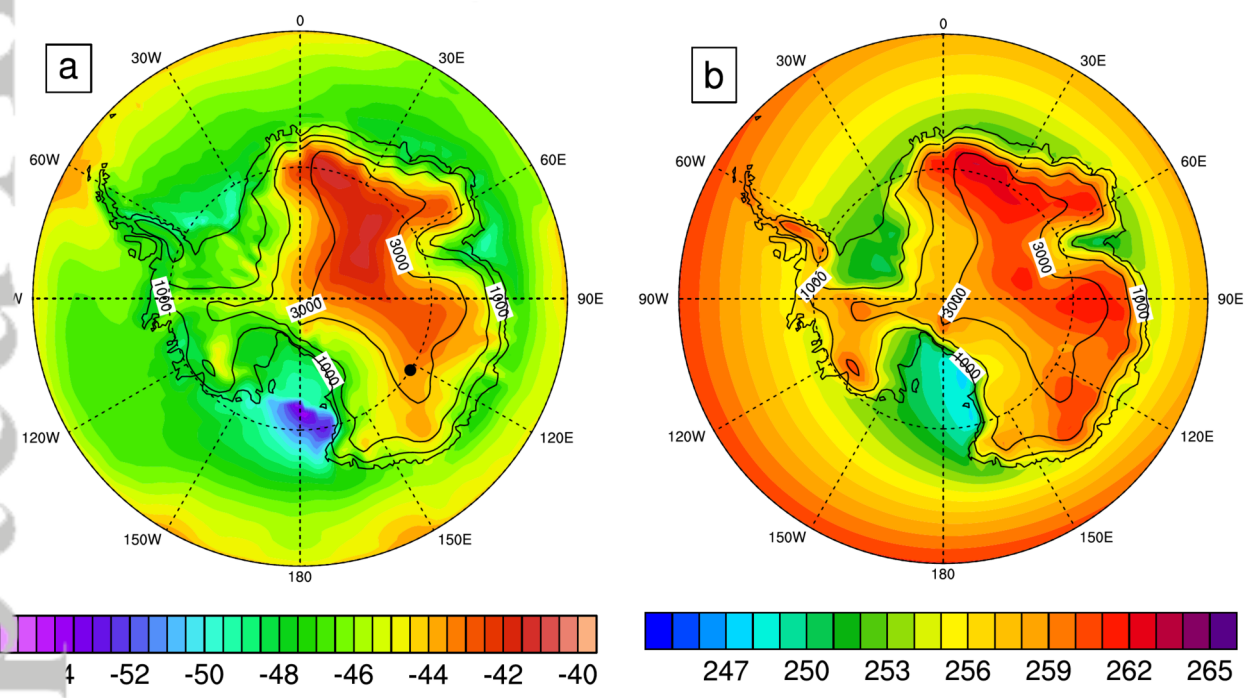
Figure 4.

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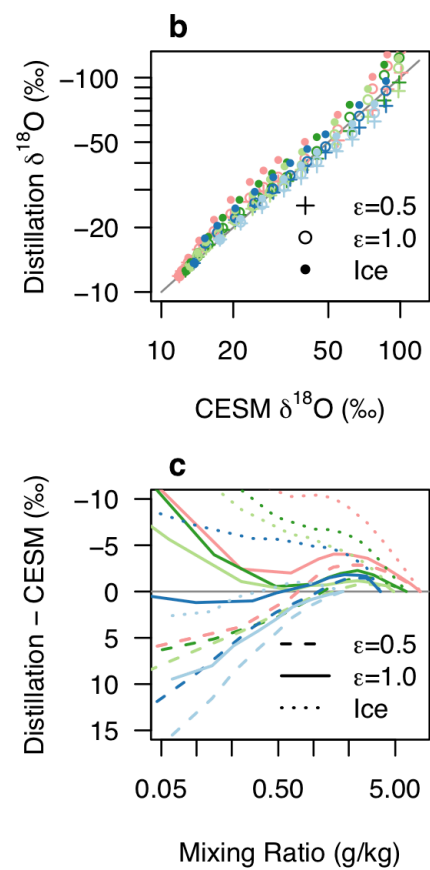
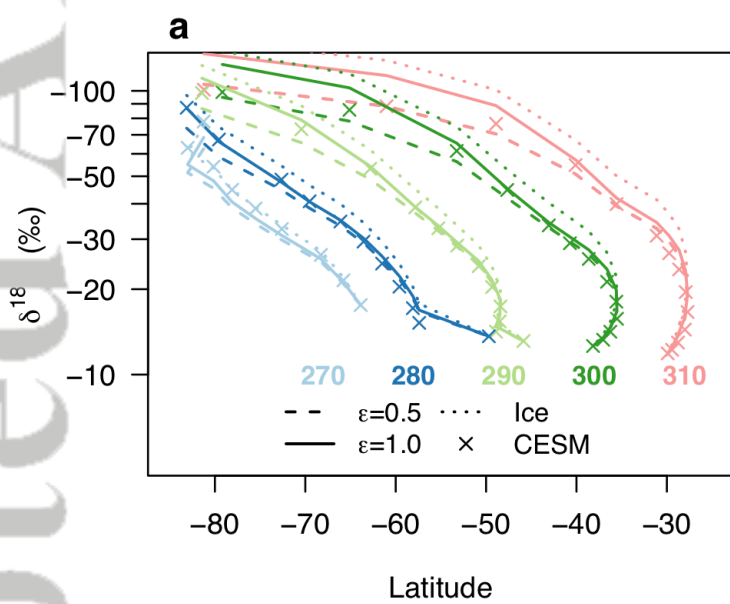




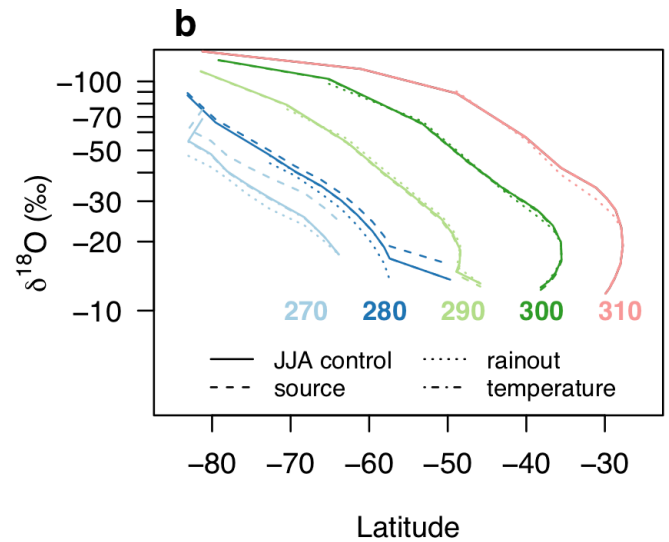
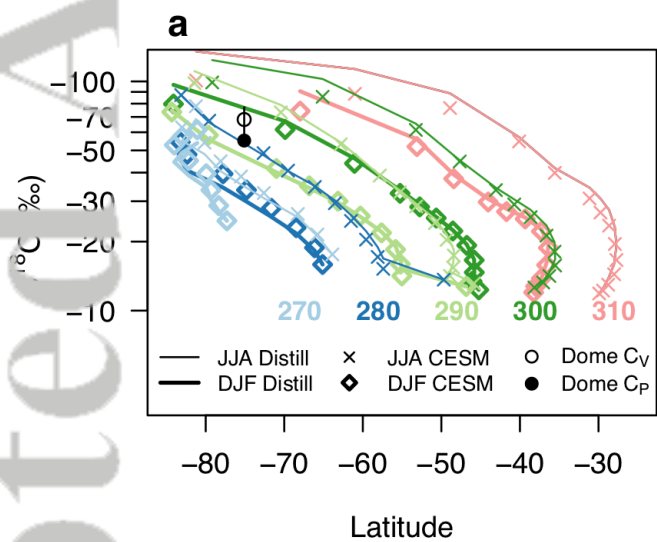
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